(For the candidates admitted from 2024–25 onwards)

M.C.A. DEGREE EXAMINATION, AUGUST 2025

First Semester

DISCRETE MATHEMATICS

Time: Three hours

Maximum: 75 marks

PART A — $(10 \times 2 = 20 \text{ marks})$

Answer ALL the questions.

- 1. Define binary relation with an example.
- 2. Give an example of an injective function.
- 3. What is well-formed formula?
- 4. Define universal quantifier.
- 5. State recurrence relation.
- 6. Write an example of a linear homogeneous recurrence relation.
- 7. What is the determinant of 2×2 matrix?
- 8. Define the rank of matrix.
- 9. Give example of an Euler graph.
- 10. Define bipartite graph.

PART B —
$$(3 \times 5 = 15 \text{ marks})$$

Answer any THREE questions.

- 11. Describe equivalence relation with two examples.
- 12. Explain principal disjunctive normal form with example.
- 13. Solve the recurrence relation: $a_n = a_{n-1} + 2$ with $a_0 = 1$.
- 14. Use Cramer's Ruleto solve: x + 2y = 5 and 3x + 4y = 6
- 15. Draw a complete graph with 5 vertices and state its properties.

PART C —
$$(5 \times 8 = 40 \text{ marks})$$

Answer ALL questions.

16. (a) Explain the types of functions with examples: injective, surejctive, bijective.

Or

- (b) Given a relation $R = \{(1, 1), (2, 2), (1, 2), (2, 1)\}$ on set $A = \{1, 2\}$. Draw its digraph and find its matrix.
- 17. (a) Construct a truth table for the formula $(P \land Q) \rightarrow (\neg R \lor P)$. Determine whether it is a tautology or contradiction.

Or

- (b) Use truth table to verify: $(P \land (P \rightarrow Q)) \rightarrow Q$ is a tautology.
- 18. (a) Differentiate between permutations and combinations with examples.

Or

- (b) How many 5-digit numbers can be formed using the digits 1 to 9 if repetition is allowed and digits must be in increasing order?
- 19. (a) Find the rank of the matrix $A = \begin{pmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \\ 1 & 0 & 1 \end{pmatrix}$.

Or

- (b) Prove Cayley-Hamilton theorem for a 2×2 matrix and verify.
- 20. (a) State and prove Euler's Theorem.

Or

(b) A graph is non-planar iff it contains a sub graph homeomorphic to K_5 or $K_{3,3}$.